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Preparation and crystal structure of a new bismuth chromate: $Bi_8(CrO_4)O_{11}$

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Abstract

Single crystals of a new bismuth chromate, $Bi_8(CrO_4)O_{11}$, were prepared by hydrothermal reaction of NaBiO₃ nH_2O in K₂CrO₄ solution. The bismuth chromate crystallizes in the monoclinic space group $P2_1/m$ with $a = 9.657(3)$, $b = 11.934(3)$, $c =$ 13.868(2)Å and $\beta = 104.14(1)^\circ$, $Z = 4$ and the final R factors are $R = 0.038$ and $R_w = 0.041$ for 3541 unique reflections. The crystal structure has a slab built up by $(CrO_4)^{2-}$ tetrahedra and distorted bismuth polyhedra which are five-fold pyramids, six-fold trigonal prisms and octahedra. The distance of lone pair from nucleus for bismuth atoms ranges from 0.29 to 1.12 Å , depending on the coordination environment. $Bi_8(CrO_4)O_{11}$ decomposes to $Bi_{14}CrO_{24}$ and a small amount of an unknown phase at 796 °C.

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Keywords: Bismuth oxide; Hydrothermal reaction; Crystal structure; Lone pair

1. Introduction

We have prepared a variety of new bismuth oxides by low-temperature hydrothermal reactions using hydrate sodium bismuth oxide, $NaBiO₃ \cdot nH₂O$ [\[1–8\]](#page-5-0). One of them, $HBi_3(CrO_4)_2O_3$ was prepared by using $Cr(NO_3)_3$ solution and its crystal structure was determined by using single crystal X-ray diffraction data [\[3\].](#page-5-0) So far several bismuth chromium oxides and oxyhydroxides have been reported, for example, $Bi_2(CrO_4)_2Cr_2O_7$ [\[9\],](#page-5-0) BiOHCrO₄ [\[10\]](#page-5-0), perovskite-type $BiCrO₃$ prepared under high pressure [\[11\]](#page-5-0) and the orthorhombic phase $Bicro₃$ prepared by an usual calcination method [\[12\].](#page-5-0) Recently, a new bismuth chromate, $Bi_6Cr_2O_{15}$, was reported [\[13\],](#page-5-0) having the unique $(Bi_{12}O_{14})^{\bar{8}n+\bar{n}}$ columns as found in $Bi_{13}Mo_{4}VO_{34}$ [\[14\]](#page-5-0). In the bismuth rich phases in the $Bi₂O₃$ –Cr₂O₃ system there are two compounds; one is the cubic sillenite-type compound [\[15\]](#page-5-0) which has the crystal structure of γ -Bi₂O₃,

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one of the four modifications of bismuth sesquioxide, and another is $Bi_{14}CrO_{24}$ which crystal structure was determined by single crystal X-ray diffraction analysis [\[16\].](#page-5-0) Except for the perovskite-type $Bicro₃$, the crystal structure of bismuth chromates is built up by $CrO₄$ tetrahedron and $Bi³⁺$ with irregular coordination environment caused by stereo active lone pair.

A new bismuth chromate, $Big(CrO_4)O_{11}$ was found on the course of investigation of hydrothermal reactions using $NaBiO₃ · nH₂O$ and the crystal structure was determined by using single crystal X-ray diffraction data. The crystal structure and thermal behavior of this new compound will be described.

2. Experimental

2.1. Sample preparation and characterization

Reddish yellow needle-like single crystals were prepared by hydrothermal reaction. $NaBiO₃ · nH₂O$ (Nacalai Tesque Inc.) was placed in a Teflon-lined autoclave (70 mL) with K_2CrO_4 (Bi:Cr = 1:2~4) and H₂O (30 mL)

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at 180° C for 4 days. The solid products were separated by centrifuging, washed with distilled water, and dried at 50° C. The products were identified by X-ray powder diffraction using Ni-filtered $CuK\alpha$ radiation. The thermal stability was investigated by TG-DTA with a heating rate of 10° C/min from room temperature to 1000° C.

2.2. Structure determination

Single crystal X-ray diffraction data were collected by using a Rigaku AFC-7R four-circle diffractometer with graphite monochromated MoK α radiation using the ω -2 θ scan technique ($D\omega = (1.42 + 0.30 \tan\theta)$ ^o). The data were corrected for Lorentz and polarization effects. Absorption effects were corrected by using ψ scans. The crystal structure was solved and refined with the computer programs from the TEXSAN crystallographic software package [\[17\]](#page-5-0). Details of the data collection and refinement are summarized in Table 1. The final positional and anisotropic thermal parameters are summarized in Table 2. Selected interatomic distances and angles are listed in [Table 3](#page-2-0). The positions of lone pairs of bismuth atoms were determined by using the laboratory-made program HYBRIDE [\[18\],](#page-5-0) based upon the research of the equilibrium position of the lone pair in the electrostatic field. A description of the principle of this program can be found in [\[19\].](#page-5-0)

 $B_{\text{eq}}^* = (8\pi^2/3)\Sigma_i \Sigma_j U_{ij} a_i^* a_j^* a_i a_j.$

Table 3 Selected interatomic distances (\AA) for Bi₈(CrO₄)O₁₁

$Cr(1)-O(6)$ $Cr(1)-O(7)$ $Cr(1)-O(11)$ Mean	1.63(3) 1.58(3) $1.63(3) \times 2$ 1.62	$Cr(2)-O(4)$ $Cr(2)-O(5)$ $Cr(2) - O(18)$ Mean	1.66(3) 1.63(3) $1.64(2) \times 2$ 1.64
$Bi(1) - O(1)$ $Bi(1) - O(2)$ $Bi(1) - O(14)$ $Bi(1) - O(18)$ Mean	2.30(3) 2.24(2) $2.16(2) \times 2$ $2.98(2) \times 2$ 2.47	$Bi(2) - O(2)$ $Bi(2) - O(3)$ $Bi(2) - O(4)$ $Bi(2) - O(10)$ $Bi(2) - O(15)$ Mean	2.09(2) 2.19(2) 2.80(3) 2.59(2) $2.36(2) \times 2$ 2.40
$Bi(3)-O(6)$ $Bi(3)-O(8)$ $Bi(3)-O(9)$ $Bi(3)-O(13)$ $Bi(3) - O(19)$ Mean	2.82(3) 2.37(2) 2.16(2) $2.79(2) \times 2$ $2.31(2) \times 2$ 2.51	$Bi(4) - O(8)$ $Bi(4) - O(9)$ $Bi(4) - O(12)$ $Bi(4) - O(20)$ Mean	2.30(2) 2.13(2) $2.75(2) \times 2$ $2.33(2) \times 2$ 2.43
$Bi(5)-O(1)$ $Bi(5)-O(3)$ $Bi(5) - O(11)$ $Bi(5)-O(12)$ $Bi(5) - O(15)$ Mean	2.36(2) 2.13(1) 2.86(3) 2.06(2) 2.36(1) 2.35	$Bi(6) - O(10)$ $Bi(6) - O(11)$ $Bi(6) - O(16)$ $Bi(6) - O(17)$ $Bi(6) - O(18)$ $Bi(6) - O(18)$ Mean	2.102(9) 2.85(2) 2.08(1) 2.15(1) 2.85(2) 2.93(2) 2.49
$Bi(7) - O(6)$ $Bi(7) - O(15)$ $Bi(7) - O(16)$ $Bi(7) - O(17)$ $Bi(7) - O(17)$ $Bi(7) - O(19)$ Mean	2.87(2) 2.11(1) 2.30(1) 2.19(1) 2.31(1) 2.93(2) 2.45	$Bi(8)-O(7)$ $Bi(8)-O(12)$ $Bi(8) - O(13)$ Bi(8)–(14) $Bi(8)-O(20)$ Mean	2.85(2) 2.24(2) 2.09(1) 2.37(2) 2.12(2) 2.33
$Bi(9) - O(5)$ $Bi(9) - O(8)$ $Bi(9) - O(14)$ $Bi(9) - O(16)$ $Bi(9) - O(19)$ $Bi(9) - O(20)$ Mean	2.99(2) 2.313(9) 2.42(2) 2.47(2) 2.10(1) 2.19(2) 2.41	$Bi(10) - O(2)$ $Bi(10) - O(9)$ $Bi(10) - O(12)$ $Bi(10) - O(13)$ $Bi(10) - O(13)$ $Bi(10) - O(14)$ $Bi(10) - O(15)$ $Bi(10) - O(19)$ Mean	2.57(1) 2.70(1) 2.87(2) 2.28(2) 2.47(2) 2.49(2) 2.74(1) 2.25(2) 2.55

3. Results and discussion

3.1. Crystal structure

The crystal structure of $Bi_8(CrO_4)O_{11}$ has a slab built up by $(CrO_4)^{2-}$ tetrahedra and Bi^{3+} coordinated by 5–8 oxygen atoms, and the slabs are stacked along the a -axis as shown in [Fig. 1](#page-3-0). In this figure the Bi–O bondings with the length of $d < 3.0$ A and the location of lone pairs are represented. The distances of the lone pairs from the nuclei are listed in Table 4. The slab of $Bi_8(CrO_4)O_{11}$ is composed of three metal layers in which the Bi layer (layer I) is sandwiched by the Cr, Bi layers (layer II). The feature of this crystal structure is similar to that of $HBi_3(CrO_4)_2O_3$ [\[3\]](#page-5-0) which has two types of slabs; one is composed of one Bi layer and two

Table 4 Distances (A) of lone pair from nucleus for bismuth atom

Layer I		Layer II	
Bi(2)	0.87	Bi(1)	0.69
Bi(3)	0.53	Bi(4)	0.50
Bi(7)	0.58	Bi(5)	1.12
Bi(10)	0.39	Bi(6)	0.54
		Bi(8)	0.82
		Bi(9)	0.29

Cr, Bi layers like that of $Bi_8(CrO_4)O_{11}$ and another is two Cr, Bi layers as shown in [Fig. 2](#page-3-0).

The various coordination environments of Bi atoms in this compound cannot be understood at first glance from [Fig. 1](#page-3-0). For easier viewing the layers I and II are separately drawn in [Fig. 3](#page-4-0) and their polyhedral representation is shown in [Fig. 4](#page-4-0). The layer I has four distinct Bi sites (Bi(2), $Bi(3)$, $Bi(7)$ and $Bi(10)$), and two types of chains connected by edge-sharing run along the b-axis; one is connected by edge-sharing $Bi(3)O_7$ and $Bi(10)O_8$ and another is by corner-sharing $Bi(2)O_6$ and $Bi(7)O_6$ octahedra. On the other hand the layer II has four types of chains connected by corner- and edge-sharing along the b-axis. Every chain is formed by edge- and/or corner-sharing polyhedra as observed in the layer I. The combinations are $Bi(6)O_6$ octahedra and $Cr(2)O₄$ tetrahedra, $Bi(5)O₅$ square pyramids and $Cr(1)O₄$ tetrahedra, Bi(4) $O₆$ trigonal prisms and $Bi(8)O_5$ pyramids, and $Bi(1)O_6$ and $Bi(9)O_6$ octahedra. Although all Bi polyhedra are strongly deformed from a regular shape, the two types of $CrO₄$ tetrahedra are almost regular ones. The mean Cr–O distances in the tetrahedra are 1.62 and 1.64 A for Cr(1) and Cr(2), respectively, and these values agree with those $(1.66-1.67 \text{ Å})$ for $HBi₃(CrO₄)₂O₃$ [\[3\]](#page-5-0) and $Bi₁₄CrO₂₄$ [\[14\]](#page-5-0).

There are four short Bi–Bi contacts in this compound. One is observed between edge-sharing $Bi(5)O₅$ pyramids as found in $Ca_4Bi_6O_{13}$ [\[20\]](#page-5-0) and the corresponding Bi–Bi distances are similar to each other $(3.601 \text{ Å}$ for this compound and 3.604 Å for $Ca_4Bi_6O_{13}$). The differences between edge-sharing $BiO₅$ pyramids of the two compounds are the shape and configuration of the pyramids. In $Ca_4Bi_6O_{13}$ the basal faces of two BiO_5 pyramids are almost square and are edge-sharing in the way that the basal faces are coplanar, while in this compound, $Bi(5)O₅$ pyramids are strongly deformed and the basal faces are not coplanar. The other short Bi–Bi contacts are observed between the layers I and II; the distances of $Bi(6) – Bi(7)$, $Bi(3) – Bi(4)$ and Bi(2)–Bi(5) are 3.424, 3.536 and 3.603 Å, respectively. For every short Bi–Bi contact the corresponding polyhedra are edge-sharing and the other edge-sharings in this compound have long Bi–Bi distance with ≥ 3.66 Å for Bi(8)–Bi(9) or $Bi(9) – Bi(10)$.

Strong deformation of Bi polyhedra which comes from a stereo active lone pair of Bi^{3+} is found in a lot

Fig. 1. Crystal structure of $Bi_8(CrO_4)O_{11}$.

Fig. 2. Crystal structure of $HBi_3(CrO_4)_2O_3$.

of Bi^{3+} oxides. The mean Bi–O distances (2.35–2.55 Å) in this compound correspond to those for the other bismuth chromates; $(2.56-2.59 \text{ Å})$ for $\text{HBi}_3(\text{CrO}_4)_2\text{O}_3$ (3), $(2.237-2.432 \text{ Å})$ for Bi₆Cr₂O₁₅ (13) and $(2.54-2.72 \text{ Å})$ for $Bi_{14}CrO_{24}$ [\[14\].](#page-5-0) [Fig. 5](#page-5-0) shows the plot of the distance of lone pair from the nucleus against mean Bi–O distance for $Bi³⁺$

in 22 complex bismuth oxides from which mixed valence compounds and perovskite-type compounds having $Bi³⁺$ in the A site are excluded. Most of Bi^{3+} oxides have the mean Bi–O distance of $2.3-2.5 \text{ Å}$ and the distance of lone pair from the nucleus is inclined to decrease with increase of the mean Bi–O distance. This tendency can be explained

Fig. 3. Layers I and II in $Bi_8(CrO_4)O_{11}$.

Fig. 4. Polyhedral representation of $Big(CrO_4)O_{11}$.

qualitatively by the coordination environment of Bi^{3+} . Generally mean Bi–O distance depends on the coordination number (CN); the Bi atom with longer mean Bi–O distance has bigger CN and smaller CN makes mean Bi–O distance shorter. Since the Bi atom with bigger CN does not have the room enough to accommodate the lone pair, the lone pair must be brought close to the nucleus. On the contrary the Bi atom with smaller CN can put the lone pair far from the nucleus. The shortest Bi–O distances (\sim 2 Å) are in the range of classical $Bi⁵⁺ - O$ bonds, accounting for a strong stereochemical effect of the lone pair that points toward the opposite direction. Actually, Bi^{3+} with the

Fig. 5. Distance of lone pair from the nucleus vs. mean Bi–O distance for various bismuth oxides. One to two correspond to $Bi(1)-Bi(10)$ in this compound: a; $Bi_6Cr_2O_{15}[13]$, b; $Bi_2Al_4O_9[24]$, c; $HBi_3(CrO_4)_2O_3[3]$, d; $Bi_{4.86}La_{1.14}O_9[23]$, e; $Bi_2W_2O_9[25]$, f; α -BiNbO₄[26], g; SrBi₂Nb₂O₉[27], h; $BaBi_2Nb_2O_9[27]$, i; $Bi_2Mo_3O_{12}[28]$, j; α - $Bi_2Ti_4O_{11}[29]$, k; β - $Bi_2Ti_4O_{11}[29]$, l-1; $Sr₂Bi₂O₅[21]$, 1-2; $Sr₂Bi₂O₅[22]$, m; $Bi₂CuO₄[30]$, n; $NaBiO₂[31]$, o; $KBiO_{2}[32]$ $KBiO_{2}[32]$, p; $Ca_{4}Bi_{6}O_{13}[20]$, q; $Bi_{2}MoO_{6}[33]$, r; $Bi_{3}SbO_{7}[34]$ $Bi_{3}SbO_{7}[34]$, s; $Bi₂WO₆[35], t; K_{0.5}Bi_{2.5}Nb₂O₉[36], u; Na_{0.5}Bi_{2.5}Nb₂O₉[36].$ $Bi₂WO₆[35], t; K_{0.5}Bi_{2.5}Nb₂O₉[36], u; Na_{0.5}Bi_{2.5}Nb₂O₉[36].$ $Bi₂WO₆[35], t; K_{0.5}Bi_{2.5}Nb₂O₉[36], u; Na_{0.5}Bi_{2.5}Nb₂O₉[36].$

Fig. 6. TG-DTA curves of $Bi_8(CrO_4)O_{11}$.

short Bi–O distance of ~ 2 Å in Ca₄Bi₆O₁₃ [19] and $Sr₂Bi₂O₅$ [21,22] (CN = 3) have a long distance of lone pair from the nucleus $(1.3-1.8 \text{ Å})$, while Bi(9) (Bi–O; 2.41 A^{\hat{A}} with CN = 6 and Bi(10) (Bi–O; 2.55 A^{\hat{A}}) with $CN = 8$ in this compound have a short distance to the lone pair $(0.29 \text{ and } 0.39 \text{ Å})$, respectively).

3.2. Thermal behavior

The TG-DTA curves of $Bi_8(CrO_4)O_{11}$ are shown in Fig. 6. No weight loss was observed in the TG curve and three endothermic peaks were observed at 796, 847 and 944 °C in the DTA curve. The strongest peak at 944 °C corresponds to the melt of the sample and the one at 796 \degree C to decomposition to $Bi_{14}CrO_{24}$ and a small amount of an unknown phase, which was confirmed by X-ray powder diffraction pattern. The weakest one appears at 847° C, but no change after cooling in the X-ray powder diffraction patterns taken above and below the temperature was observed. The corresponding peak was not observed during the cooling. This weak endothermic peak may be related to the unknown phase.

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